













- Pyramidal horn a x b dimensions where id propagated the fundamental mode  $TE_{10}$ . Aperture A x B, with A>a and B>b.
- Fields in the aperture are an expanded version from the fields within waveguide:

$$\vec{E}_{ay} = \hat{y} E_0 \cos\left(\frac{\pi x}{A}\right) e^{-j \cdot \beta \cdot \Delta R}$$

• The electrical field amplitude in the horn aperture changes as a cosine in the x direction and keeps uniform along y direction.



• Finally the electrical field in the aperture can be written as:

$$\vec{E}_{ay} = \hat{y}E_0 \cos\left(\frac{\pi x}{A}\right)e^{-j\cdot\beta\cdot\left[\left(x^2/2R_1\right) + \left(y^2/2R_2\right)\right]}$$

• Where  $E_0$  is amplitude of the electrical field, and  $\beta$  is the phase constant which in the aperture is equal to the propagation constant in the free space if  $A >> \lambda$ :

$$\beta = k_0 \sqrt{1 - \left(\frac{\lambda}{2A}\right)^2} \approx k_0 = \frac{2\pi}{\lambda}$$

With  $\lambda$  the wavelength.



## Pyramidal horn



- Radiation pattern of the horn antennas are called universal radiation patterns, because they can be used for any A and B.
- They are function of the maximum phase errors that exist in the aperture.
- These maximum phase errors are *t* for the H-plane and *s* for the Eplane, they are expressed as a multiple of  $2\pi$  radians, and they are calculated from the maximum phase error  $\delta_{max}$  in the aperture:

$$\delta_{\max} = \frac{k_0}{2R_1} \left(\frac{A}{2}\right)^2 = \frac{2\pi}{\lambda} \frac{A^2}{8R_1} = 2\pi t \Longrightarrow t = \frac{A^2}{8\lambda R_1}$$
$$\delta_{\max} = \frac{k_0}{2R_1} \left(\frac{B}{2}\right)^2 = \frac{2\pi}{\lambda} \frac{B^2}{8R_2} = 2\pi s \Longrightarrow s = \frac{B^2}{8\lambda R_2}$$







- With lobes at very high levels when aperture is large (about -19dB).
- The radiation pattern are calculated from the universal radiation patterns, which depend on the maximum phase error in the aperture *s*:

$$s = \frac{a^2}{2\lambda L}$$





• Electrical field phase in the aperture as a wave with spherical phase front.











Reflector antennas can be analysed using different methods which provide similiar results:

• Geometrical Optics (GO): It allows to calculate the fields over the aperture and then the radiated fields using the equivalent principles. It is based on the Fermat principle and the Snell's laws.







**Physical Optics (PO):** It calculates the radiated fields with the induced currents over the metallic reflector.



**Geometrical theory diffraction (GTD):** It provides us the best results for the radiated fields, overall for the secondary far lobes. They are analysed the direct rays and the diffracted rays in the edges.







## Reflector types (II)

**Cassegrain reflector:** It is a combination of a parabolic primary concave mirror and a hyperbolic secondary convex mirror. They are usually used in optical telescopes where a high gain is required.

**Cassegrain reflector:** It is similar to the previous type, but instead of using a primary mirror with parabolic shape, it is used an elliptical mirror.

















Multifeeding

**Conformal surfaces** 





## Conformal reflectors (I)



• The specifications are coverage contours in dBW

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- The design consists on changing the shape of the reflector.
- A concrete surface must be set up, starting from a concrete canonical design: Paraboloidal, Cassegrainian...







## Aperture optimization

• Conforming a reflector can improve the aperture efficiency.

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**SSR** 

- The goal is to get more uniform amplitude distributions in the aperture.
- The phase front must be plane in the aperture.
- Two constraints and two design elements: reflector and subreflector.



